



# Deep Transfer Mapping for Unsupervised Writer Adaptation

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## **Introduction**

## **Style Transfer Mapping**

## Motivation and the Proposed Method

## **Mathematic Experiments and Analysis**

## **Conclusions**



### • A main challenge for handwriting recognition:

#### The large variability of distributions across training and different test data

- Different writing styles of different writers
- Different writing tools (e.g. different pens or electronic writing devices)
- Different writing environments (e.g. normal or emergency situations)

Written characters of two writers.

## Introduction



Domain adaption: a form of transfer learning
 Adapt the base classifier to each domain in the test dataset



- Recent methods: mainly based on deep learning
  - Fine tuning with target domain data
  - Learning domain invariant representations (features)
  - Project source or target domain data to align the distribution

## Style Transfer Mapping



### Style transfer mapping (STM)

Main idea: project the target domain (test) data to balance the data distribution

$$p(x_s) \neq p(x_t)$$
$$\hat{x}_t = A_t x_t + b_t$$
$$p(x_s) \approx p(\hat{x}_t)$$

Learning classifier on  $x_s$  and apply  $\hat{x}_t$  to the base classifier

• Learning of the projection  $(A_t \text{ and } b_t)$ 

$$min_{A \in \mathbb{R}^{d \times d}, b \in \mathbb{R}^{d}} \sum_{i=1}^{n} f_{i} \|As_{i} + b - t_{i}\|_{2}^{2} + \beta \|A - I\|_{F}^{2} + \gamma \|b\|_{2}^{2}$$

**Source points**  $s_i$ : features in the target domain, i.e.,  $x_t$ 

**Target points**  $t_i$ : prototype (LVQ) or mean (MQDF) for class  $y_i$  ( $y_i$  is the label of sample  $s_i$ )



## Style Transfer Mapping

**Solution:** a convex quadratic programming problem, has a closed-form solution

$$A = QP^{-1}, b = \frac{1}{\hat{f}}(\hat{t} - A\hat{s})$$

$$Q = \sum_{i=1}^{n} f_{i}t_{i}s_{i}^{\mathrm{T}} - \frac{1}{\hat{f}}\hat{t}\hat{s}^{\mathrm{T}} + \beta I \quad P = \sum_{i=1}^{n} f_{i}s_{i}s_{i}^{\mathrm{T}} - \frac{1}{\hat{f}}\hat{s}\hat{s}^{\mathrm{T}} + \beta I \quad \hat{s} = \sum_{i=1}^{n} f_{i}s_{i} \quad \hat{t} = \sum_{i=1}^{n} f_{i}t_{i} \quad \hat{f} = \sum_{i=1}^{n} f_{i} + \gamma$$

### Dealing with unsupervised adaptation

- Using the pseudo labels, predicted by the base classifier
- − Iteration method: base classifier → pseudo label → adaptation → better pseudo label → adaptation → .....

#### Extend to convolutional neural networks (CNNs)

Main idea: perform adaptation on the deep features

f(x): CNN feature extractor

$$x_s = f(x_s), \qquad x_t = f(x_t)$$

[Xu-Yao. Zhang et al., writer adaptation with style transfer mapping. TPAMI'13]

[Xu-Yao. Zhang et al., online and offline handwritten Chinese character recognition: a comprehensive study and new benchmark. PR'17]



### Traditional adaptation methods with CNN

- Consider only the fully connected layers
- Perform adaptation only on one layer

### Motivations

- Adaptation on both fully connected layers and convolutional layers
- Perform adaptation on multiple (or all) layers of the base CNN
- Adaptation method for fully connected layers

STM based on the deep features of the layer (unsupervised adaptation)

- Adaptation methods for convolutional layers
- Use a linear transformation to project the target domain data for aligning the data distributions
- Propose four variations of linear transformation, which are based on different assumptions of the space relation in the feature maps



#### Fully associate adaptation (FAA):

- Output of a convolutional layer for an input  $x_i$ 

$$o_i = \left\{ d_{cjk} \right\}_{c=1, j=1, k=1}^{c=C, j=H, k=W}$$

c, j, k: index of the feature maps, rows, and columns in each feature map

- Assumption: all positions of (c, j, k) are related to each other
- Method: expand  $o_i$  to a long vector  $v_i$  with dimension CHW, and learn a transformation  $A \in R^{CHW \times CHW}$ ,  $b \in R^{CHW}$  by STM
- $v'_i = Av_i + b$ ,  $(v'_i)_j = \sum_{k=1}^{CHW} A_{jk}(v_i)_k + b_j$ , each position j in  $v'_i$  are related to all positions in  $v_i$





- > Partly associate adaptation (PAA):
- Assumption: positions within the same feature map are related to each other, but the feature maps are mutually independent
- Method: expand each feature map to a vector with dimension HW, and learn a transformation  $A_c \in R^{HW \times HW}$ ,  $b_c \in R^{HW}$  for each feature map c separately by STM
- Transformation  $A_c$ ,  $b_c$  ensures the relation of positions within a feature map, learn  $A_c$ ,  $b_c$  separately ensures the independence between the feature maps



## Motivations & Methods



- > Weakly independent adaptation (WIA):
- Assumption: all positions (c, j, k) in  $o_i$  are independent to each other
- Learn a transformation  $a, b \in R$  for each position (c, j, k) separately by STM

$$- (o'_i)_{c_0, j_0, k_0} = a(o_i)_{c_0, j_0, k_0} + b$$

$$- \min_{a,b\in R} \sum_{i=1}^{N_t} f_i \left( a(o_i)_{c_0,j_0,k_0} + b - (t_i)_{c_0,j_0,k_0} \right)^2 + \beta (a-1)^2 + \gamma b^2$$



## Motivations & Methods



- Strong independent adaptation (SIA):
- Assumption: all positions are independent to each other and the positions within the same feature map share a same linear transformation
- Similar to the linear projection in the batch normalization (BN) layer
- Learn a transformation  $a, b \in R$  for each feature map separately by STM

$$min_{a,b\in R} \sum_{i=1}^{N_t} \sum_{j=1}^{H} \sum_{k=1}^{W} f_i (a(o_i)_{c_0,j,k} + b - (t_i)_{c_0,j,k})^2 + \beta (a-1)^2 + \gamma b^2$$

$$a_1, b_1$$

$$a_2, b_2$$

$$\vdots$$



#### > Analysis and comparison

Adaptation Methods	FAA	ΡΑΑ	WIA	SIA
Assumption	All positions related	Inner feature map related	All positions independent	All positions independent & parameter sharing
Feature Dimension	CHW	HW	1	1
Matrix Size	$CHW \times CHW$	$HW \times HW$	$1 \times 1$	$1 \times 1$
Transformation Number	1	С	CHW	С
<b>Total Parameters</b>	CHW(CHW+1)	CHW(HW + 1)	2CHW	2 <i>C</i>

- Complexity & Flexibility: FAA > PAA > WIA > SIA
- Computation & Memory efficiency: SIA > WIA > PAA > FAA



### Deep transfer mapping (DTM)

#### Perform adaptation on multiple layers in a deep manner

#### > Algorithm

- 1. Select a group of layers *L* on which to perform adaptation
- 2. From bottom to top layers in *L*, perform adaptation on the specific layer with the proposed adaptation methods, but keep the other layers unchanged
- 3. After adaptation on each layer, insert an linear layer after it and set the weights and bias of the linear layer as the solved A and b

### Advantages of DTM

- More powerful for flexibly aligning the distributions between the domains
- Captures more comprehensive information and minimize the discrepancy of distributions under different abstract levels



#### Datasets

Dataset	Dataset Info	#Sample (in 3755- class)	#Writers (domains)		
Training Set	CASIA OLHWDB 1.0-1.2	2,697,673	1020		
Test Set	On-ICDAR2013 Competition	224,590	60		
Adaptation Set	Unlabeled samples from each domain (writer) in test set				

Online handwritten Chinese characters. The samples of one writer stored in one single file, can be viewed as a domain.





## **Experiments & Analysis**

Layer ID	Layer Type	Parameter	Pooling	Drop Rate
0	input	$8(32 \times 32)$	#	0.0
1	conv	$50(3 \times 3)$	#	0.0
2	conv	$100(3 \times 3)$	$2 \times 2$	0.1
3	conv	$150(3 \times 3)$	#	0.1
4	conv	$200(3 \times 3)$	$2 \times 2$	0.2
5	conv	$250(3 \times 3)$	#	0.2
6	conv	$300(3 \times 3)$	$2 \times 2$	0.3
7	conv	$350(3 \times 3)$	#	0.3
8	conv	$400(3 \times 3)$	$2 \times 2$	0.4
9	FC	900	#	0.5
10	FC	200	#	0.0
11	softmax	3755	#	#

Base classifier: 11 layers 97.55% accuracy on test set

#### • Different adaptation methods for Convolutional layers

Four adaption methods on the same convolutional layer #8

Methods	without	FAA	PAA	WIA	SIA
Test Acc (%)	97.55	97.91	97.71	97.69	97.62
ERR (%)	0	14.69	6.53	5.71	2.86



### • Adaptation property of different layers in CNN

#### TABLE III Adaptation Performance for Different Layers in CNN.

Layer ID	1	2	3	4	5	
Test Acc (%)	97.51	97.57	97.61	97.61	97.63	
ERR (%)	-1.63	0.82	2.45	2.45	3.27	Adaptation
Layer ID	6	7	8	9	10	
Test Acc (%)	97.67	97.67	97.69	97.85	97.91	
ERR (%)	4.90	4.90	5.71	12.24	14.69	

From bottom to top layers, the adaptation performance increases

- Bottom layers extract general features, which are applicable across different domains, thus the promotion are not obvious after adaptation
- Top layers occupy abstract features, which are more domain specific, thus adaptation is helpful for such layers



### Deep transfer mapping

#### TABLE IV Adaptation Performance for Deep Transfer Mapping.

Layer ID	without	8	$8 \rightarrow 9$	$8 \rightarrow 9 \rightarrow 10$
Test Acc (%)	97.55	97.91	98.00	98.02
ERR (%)	0	14.69	18.37	19.18

- DTM can further boost the performance of the base classifier
- DTM still has some limitations, the promotion is not obvious when adopt overmuch adaptations



- Unsupervised domain adaptation to alleviate the writing style variation, assuming each writer has an consistent style
- Four variations of adaptation methods for convolutional layers, assuming different space relations in the output of convolutional layers
- Deep transfer mapping (DTM) method to conduct adaptation on multiple (or all) layers of CNN, to better align the data distributions of different styles
- Remaining Problems
  - What is the best way of adaptation for deep neural networks
  - How to adapt in the case of small sample in adaption/testing (currently 3,755 samples per writer)
  - Theoretical modeling of within/between-writer style variation
  - Continuous adaptation of classifier



# **Thanks for your attention!**