



Poset – partially  
ordered set

# Poset Description of Grid Features and Application to Off- Line Signature Verification

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# Introduction to the field

- Handwriting: A behavioral way for resolving the problem of recognizing writers
- Lots of Applications: Forensics, Security, e-business, e.t.c.
- Handwriting based verification can be categorized to :
  - ✓ Context Dependent
    - Signatures or pre-defined text
  - ✓ Context Independent
- Signatures: The common way to declare our identity.
  - ✓ On-line and/or Off-line

# The basic idea

- Presented a couple of years ago
- A feature extraction method with applications to:
  - ✓ Signatures
  - ✓ Coding of words and sentences
- Produced encouraging results (EER)
- Based on the probabilistic measure of predefined pixel transitions

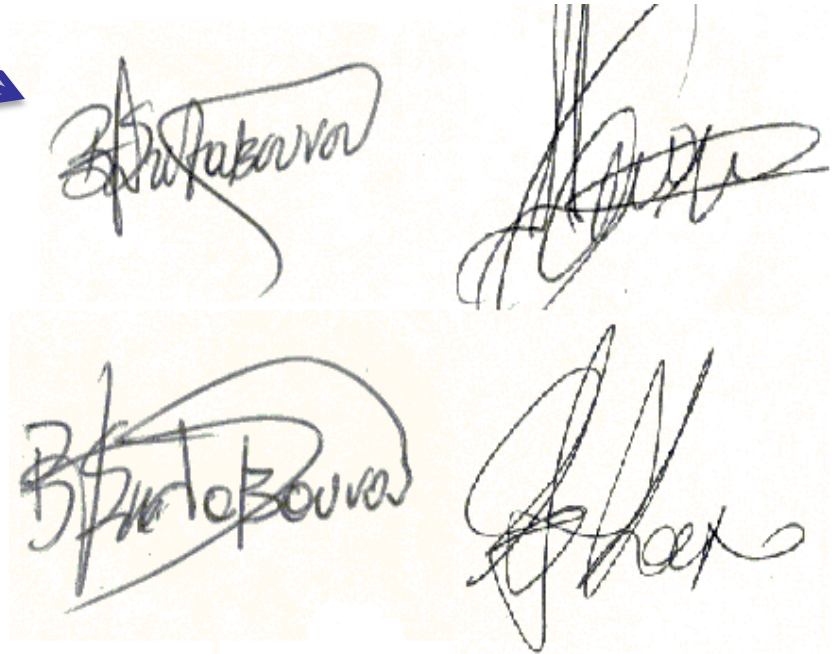
# The new proposal

- We improved over the old feature extraction method
- Provide a new feature modeling:
  - ✓ Combine concepts from information and communication theory
  - ✓ Consider the old features as symbols
  - ✓ Use sequences of symbols to create events
  - ✓ Estimate their first order probabilities
- The outcome of this procedure is an attempt to model the handwriting process in concordance with basic elements of information and coding theory.

# Databases

- **CORPUS1:** Greek database with 69 writers.

- ✓ **Under** enrichment and restructuring
- ✓ **Each writer:** 105 samples (genuine) and 21 skilled forgeries
- ✓ **Development time:** One year



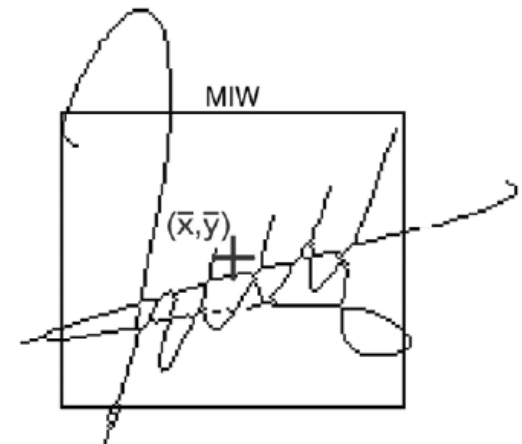
- **CORPUS2:** GPDS300

- ✓ Well known
- ✓ **Each writer:** 24 samples (genuine) and 28 skilled forgeries

No picture is displayed  
due to license restrictions

# Signature Preprocessing

- Typical preprocessing algorithms were applied:
  - ✓ Signature Segmentation
  - ✓ Thresholding with Otsu's Algorithm
  - ✓ Thinning or skeletonization
    - ☞ *Thinning was not the best choice for GPDS300*
  - ✓ Finding 'center of mass' of each signature
  - ✓ Most informative window (MIW)
- Feature extraction with respect to MIW section



# Feature Extraction: Pixels...

- Consider a 3x3 pixel window-mask.
- Locate its starting point at the **3,1** coordinates

1,1	1,2	1,3
2,1	2,2	2,3
<b>3,1</b>	3,2	3,3

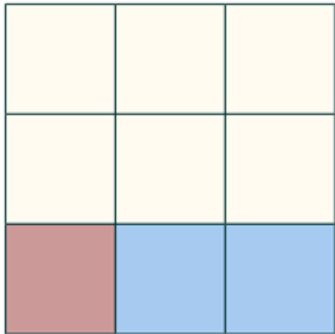


# Feature Extraction: Pixels...

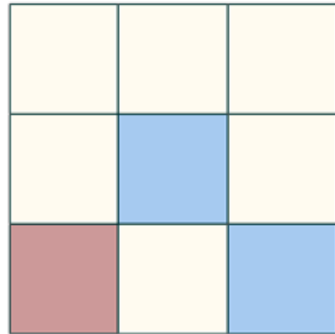
- Create connected binary patterns of **3** pixels
  - a) **Starting** from **3,1**.
  - b) **Ending** at any pixel with Chebyshev (chessboard) distance **equal to two (2)**.
- Eight (8) primary patterns  $BG_i, i=\{0:7\}$

<b>1,1</b>	<b>1,2</b>	<b>1,3</b>
<i>2,1</i>	<i>2,2</i>	<b>2,3</b>
<b>3,1</b>	<i>3,2</i>	<b>3,3</b>

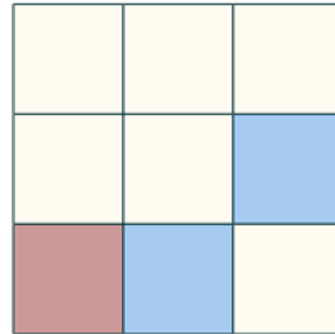
# The Eight Primary Binary Grids ( $BG_i$ )



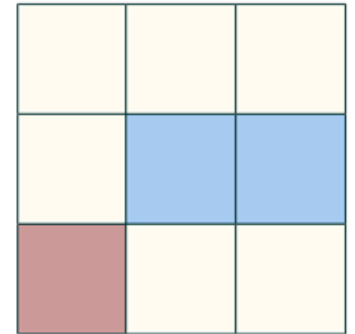
$BG_0$



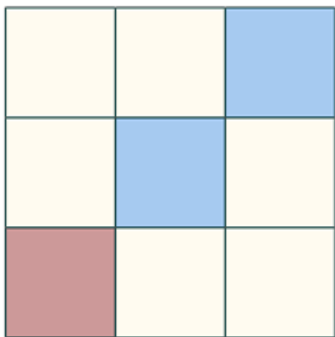
$BG_1$



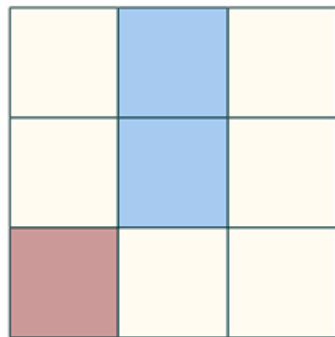
$BG_2$



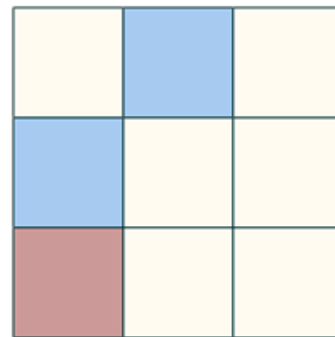
$BG_3$



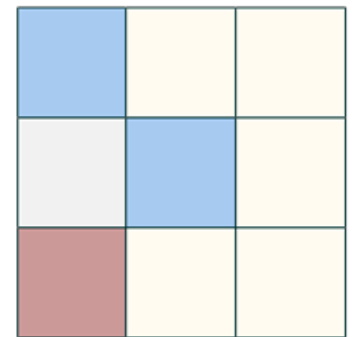
$BG_4$



$BG_5$



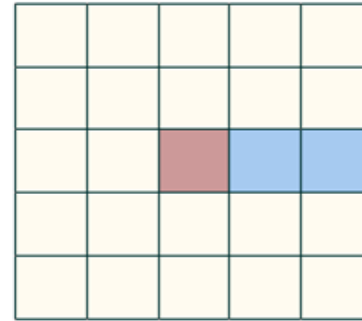
$BG_6$



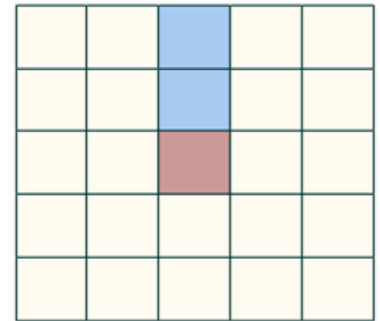
$BG_7$

# Rotating BG<sub>i</sub>s

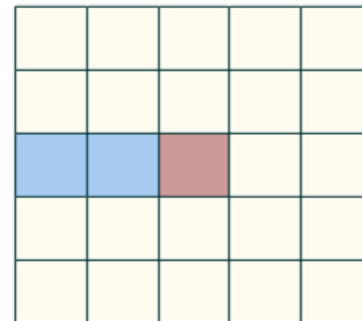
- Each of the BG<sub>i</sub>s is rotated by 90, 180 and 270 degrees
- The result is now positioned within a **5x5 grid**
- An example is provided to the right for the BG<sub>0</sub>
- Total number of alphabet symbols equals to 32



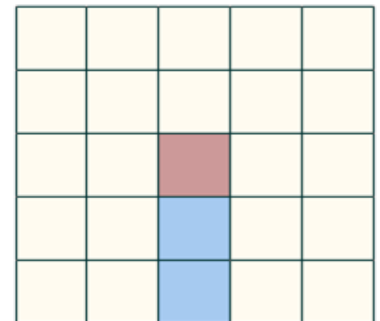
$\{BG_0\}^0$



$\{BG_0\}^1$

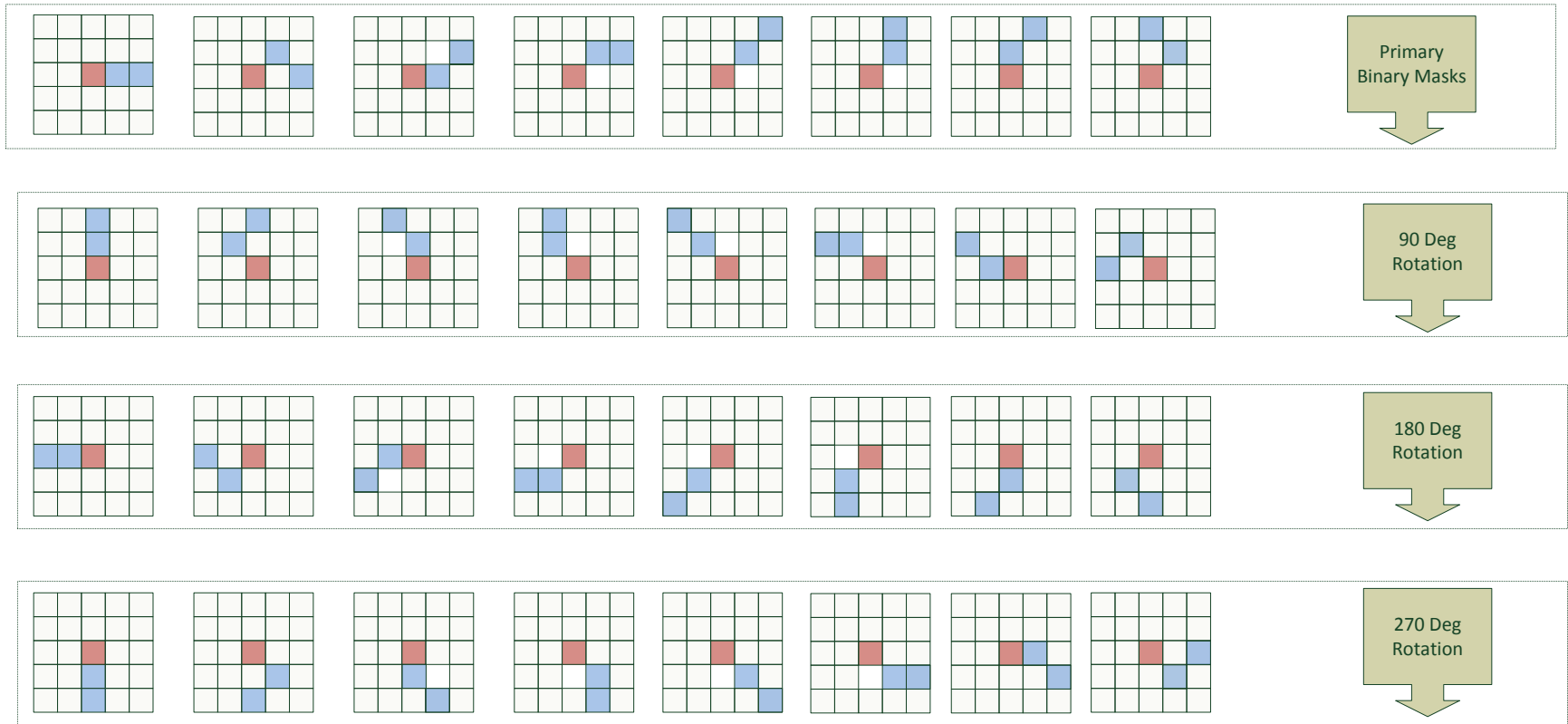


$\{BG_0\}^2$




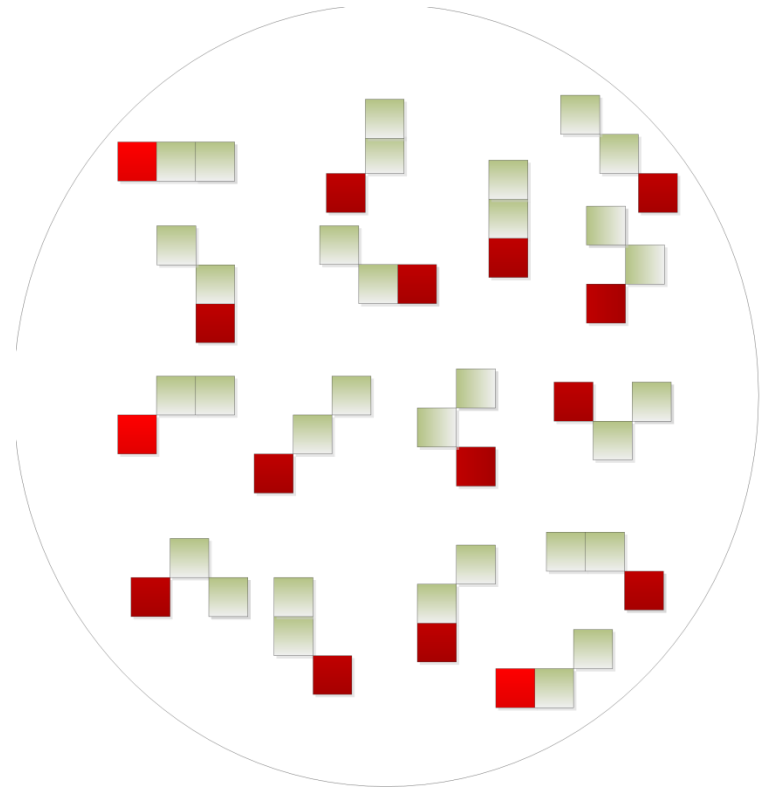
$\{BG_0\}^3$

# The Entire 32 Element Set



# Modeling signature pixels

- Let us consider a collection of the 32-element set 
  - A set of predefined **symbols**.
- The feature extraction process can be modeled as a ***discrete space – discrete alphabet source***
  - **Simple events:** *Presence of a symbol*
  - **Compound events:** *Presence of a symbol combination*



# Features and Grids (a)

- The number of combinations that the 32 elements can provide is almost immeasurable ( $\sim 10^{27}$ ).
- A reduction is applied to the number of extracted events by employing the functional and convenient concept of set partitioning.

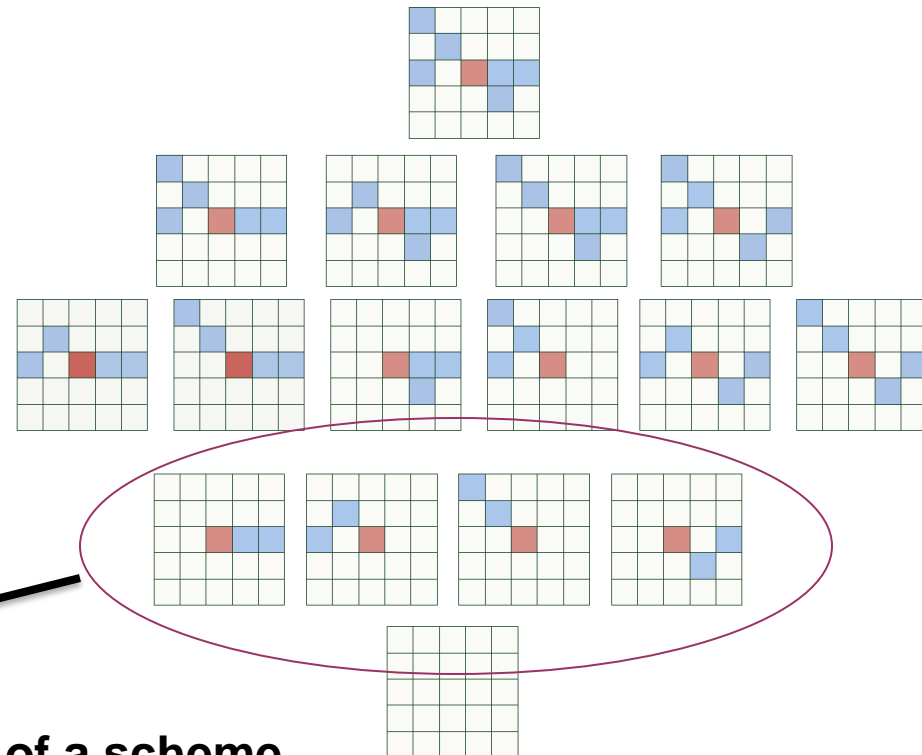
# Features and Grids (b)

- The elements of the 32 element set are grouped, (partitioned) into subsets of eight tetrads
  - *number of possible combinations still very large*
- Each one of them is called a **scheme**
- Further reduction is achieved by selecting only **orthogonal** schemes
  - *Orthogonal schemes have their tetrad members arranged in such a way that no any other member can be described by the linear combination of the three remaining*
- Now, the total number of schemes is 2587

# Power-Set

The set of all subsets of a set  $A$  is called the *power set* of  $A$  and denoted as  $\wp(A)$  or sometimes as  $2^A$ .  
For example, if  $A = \{a, b\}$ ,  $\wp(A) = \{\emptyset, \{a\}, \{b\}, \{a, b\}\}$ .

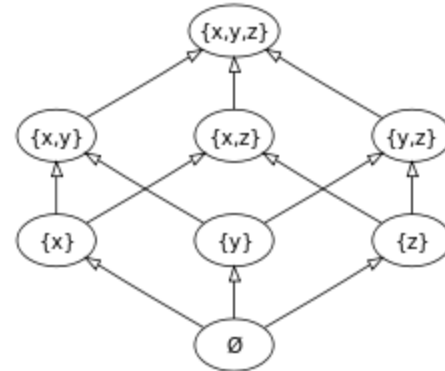
- Given a scheme:
  - For each one of its **eight** tetrads, create their powerset.



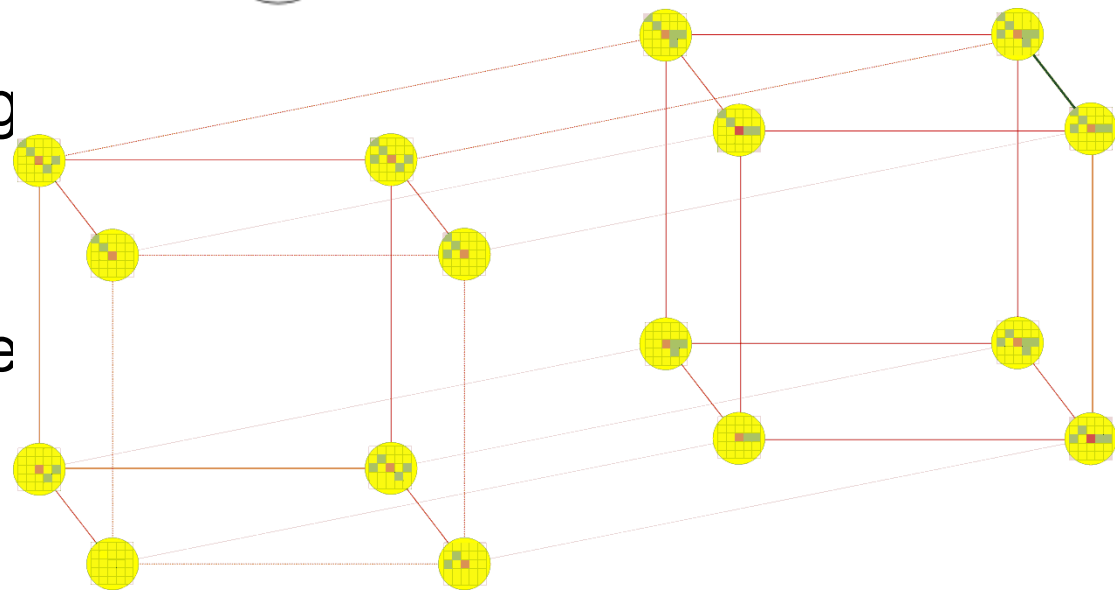
***One of the eight tetrads (layer) of a scheme and its corresponding (sixteen element) powerset.***



# Partially Ordered Set – (Poset)



The elements of the power set of the set  $\{x, y, z\}$  ordered in respect to inclusion (wikipedia)

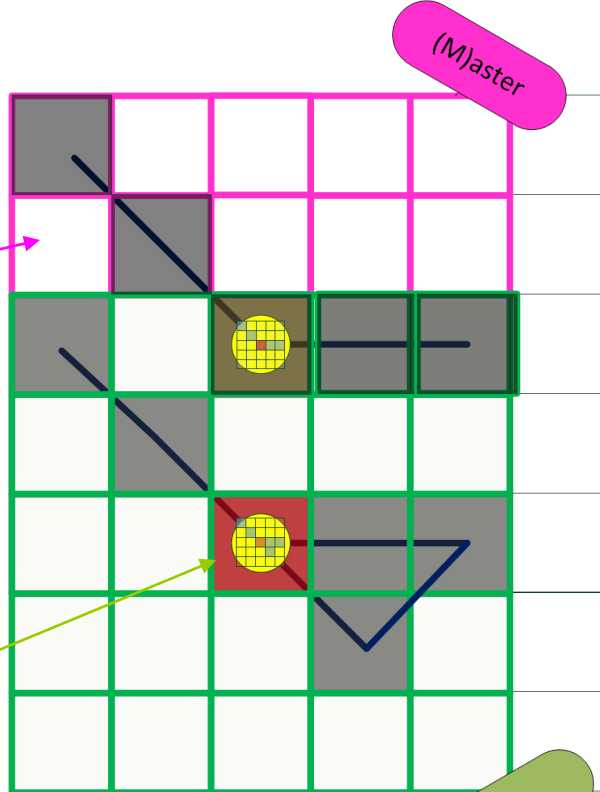


The power set of a 4-element set **ordered** by inclusion

- The concept of ordering:
  - Each one of the eight power-sets is evaluated by ordering its elements with respect to **inclusion**.
  - Detected features are those designated as links on the poset grid.

# Poset Features

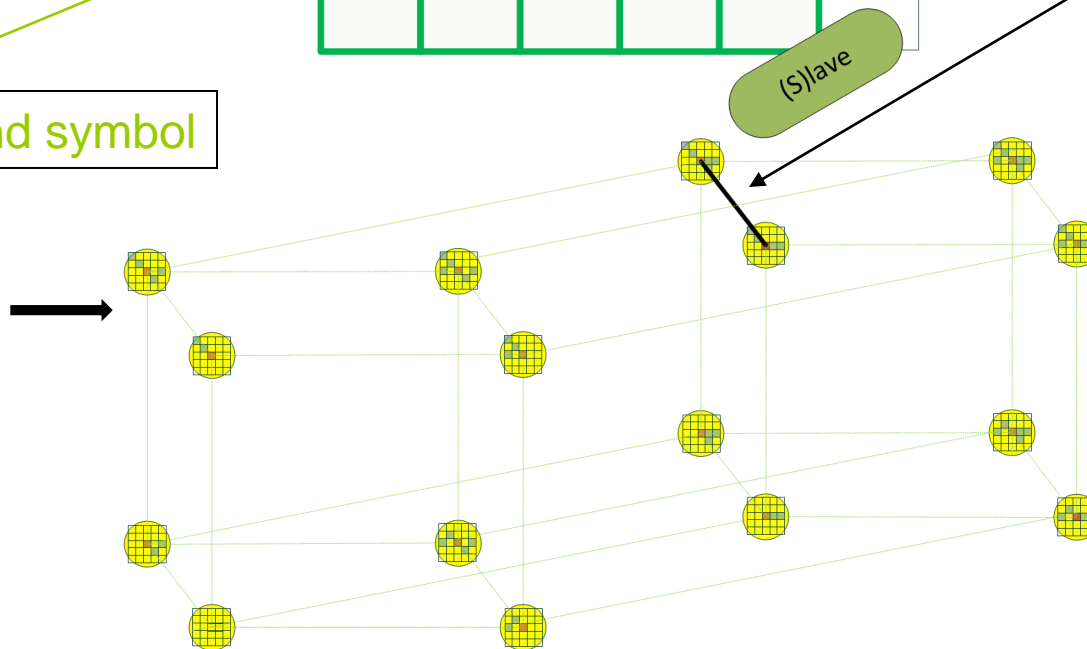
Detection of a symbol



Poset features are detected using enlarged window

Detection of a second symbol


For each edge there is a corresponding probability index which is updated when the specific ordering of symbols occurs



Feature found

# Feature Dimensionality

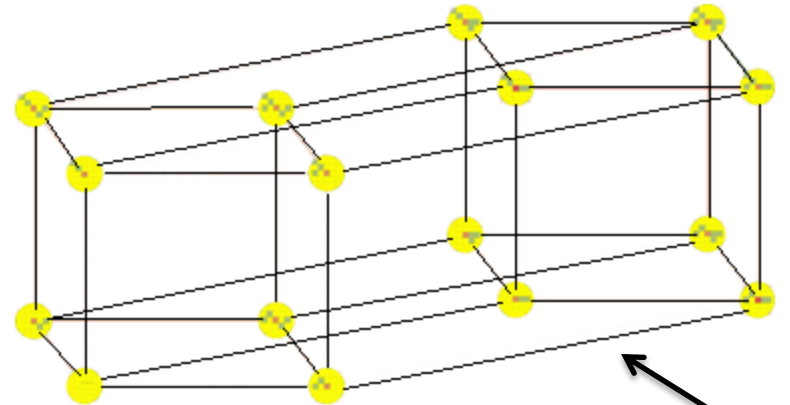
Number of Features

(i) for each tetrad = **32** 

(ii) There are **8** tetrads  $32 \times 8 = \mathbf{256}$

(iii) In addition to the whole signature image, each signature is partitioned in **4** segments ( $1+4=\mathbf{5}$ )

Thus feature dimensionality is:  
 $5 \times 256 = \mathbf{1280}$



$12 + 12 + 8 = 32$



$1 + 4 = 5$

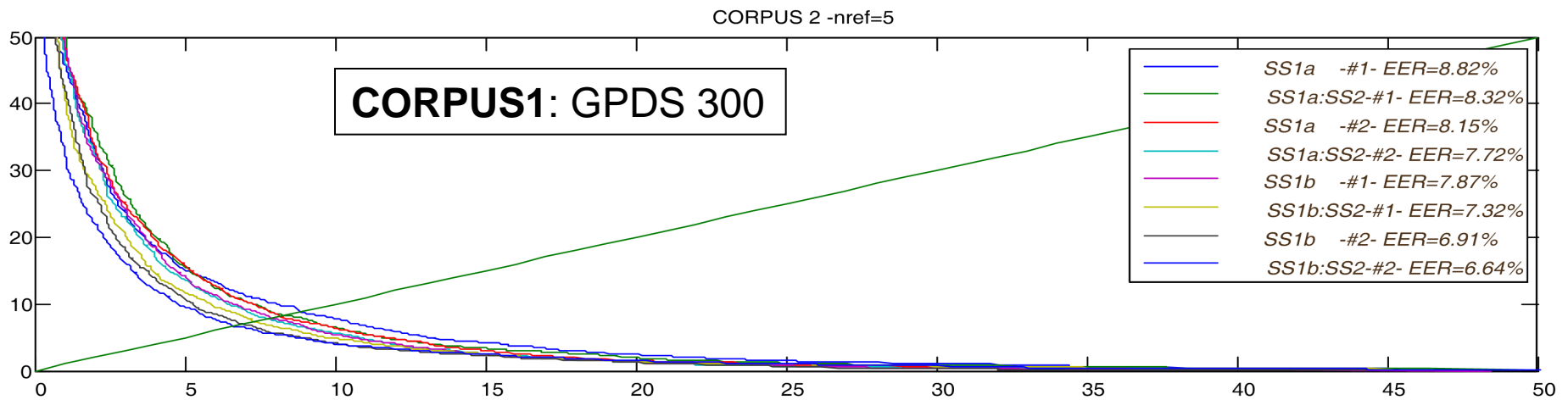
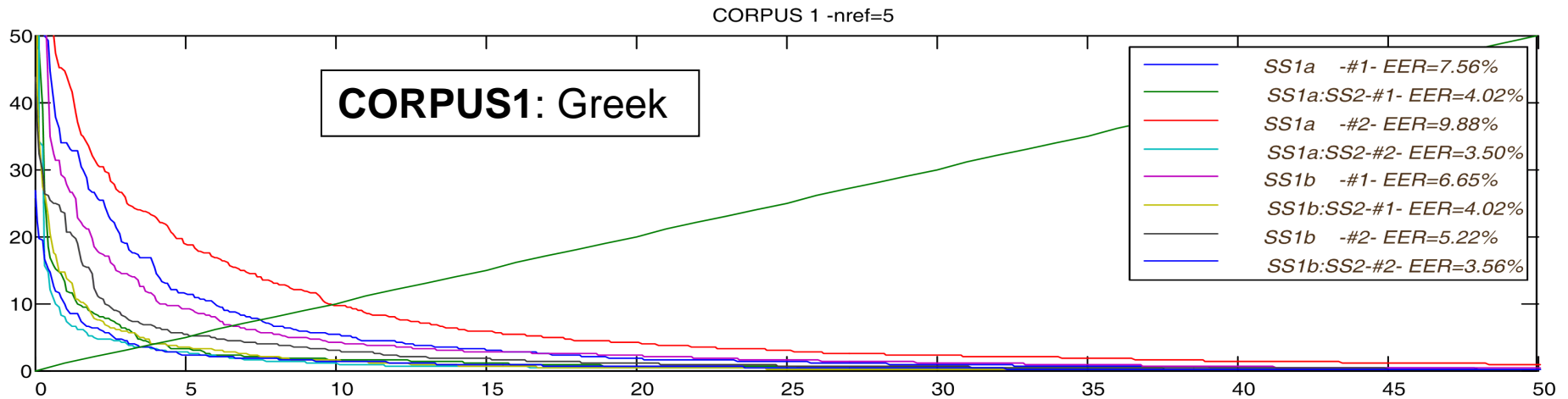
# Verification Scheme

- Writer Dependent (WD) approach
- For each writer,  $\#nref$  reference samples of genuine along with an equal number of simulated-forgery signature samples are randomly chosen in order to train the classifier
- The classifier is a hard-margin two class support vector machine (SVM) classifier using radial basis kernel
- The SVM outputs:
  - *binary class decision*
  - *a score value (equal to the distance of the tested sample from the SVM separating hyperplane)*
- There is a wide area of rbf sigma values that the system provide the reported results

# Verification Scheme

- Evaluation of the verification efficiency of the system is accomplished with the use of a global threshold applied on the overall SVM output score distribution
- Calculation of the FAR, FRR and EER

# Results – ROC, EER



# Results – Comparisons

## Corpus1

	<b>FRR</b>	<b>FAR</b>	<b>EER</b>
K. Tselios, [11] IET '12	-	-	9.16
K. Barkoula, [21] AFHA'13	3.29	2.18	2.79
<b>Proposed: random scheme #1</b>	<b>2.97</b>	<b>4.11</b>	<b>3.51</b>
<b>Proposed: random scheme #2</b>	<b>3.44</b>	<b>3.78</b>	<b>3.56</b>

# Results – Comparisons Corpus2

Primary Author	FRR	FAR	EER
M. Ferrer, [27]	13.40	12.60	13.12
J. F. Vargas, [10]	12.06	10.53	9.02
L. Batista, [24]	16.81	16.88	-
G. Pirlo, [25]	-	-	4.6
V. Niguen, [27]	-	-	17.25
M. B. Yilmaz [28]	-	-	15.41
R. Kumar, [14]	-	-	13.76
J. R. Solar [29]	-	-	15.30
K. Tselios, [11] IET '12	-	-	12.32
K. Barkoula, [21] AFHA'13	5.23	13.03	9.04
<b>Proposed: Random scheme #1</b>	<b>4.30</b>	<b>11.56</b>	<b>7.72</b>
<b>Proposed: Random scheme #2</b>	<b>9.22</b>	<b>4.61</b>	<b>6.65</b>



# Conclusions

- A new modeling of a feature extraction method
- Ordering of power set with respect to inclusion
- The method seems promising
- There are still many issues that we must address

Among others 

# Conclusions - issues to be addressed



- Writer Independent (WI) method – Dissimilarity framework
- Definition of first and higher order transition probs
- Application to writer verification problems
- Signature Complexity and Stability issues
  - ❖ *Preliminary results have been presented at AFHA 2014*
- Selection of the optimal scheme:
  - ❖ *sparse representation approach (preliminary results)*
- Use of multi-resolution windows

— . . . . .

Thank you

Questions?