

# Multiscale Analysis of Discrete Contours for Unsupervised Noise Detection

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## Abstract

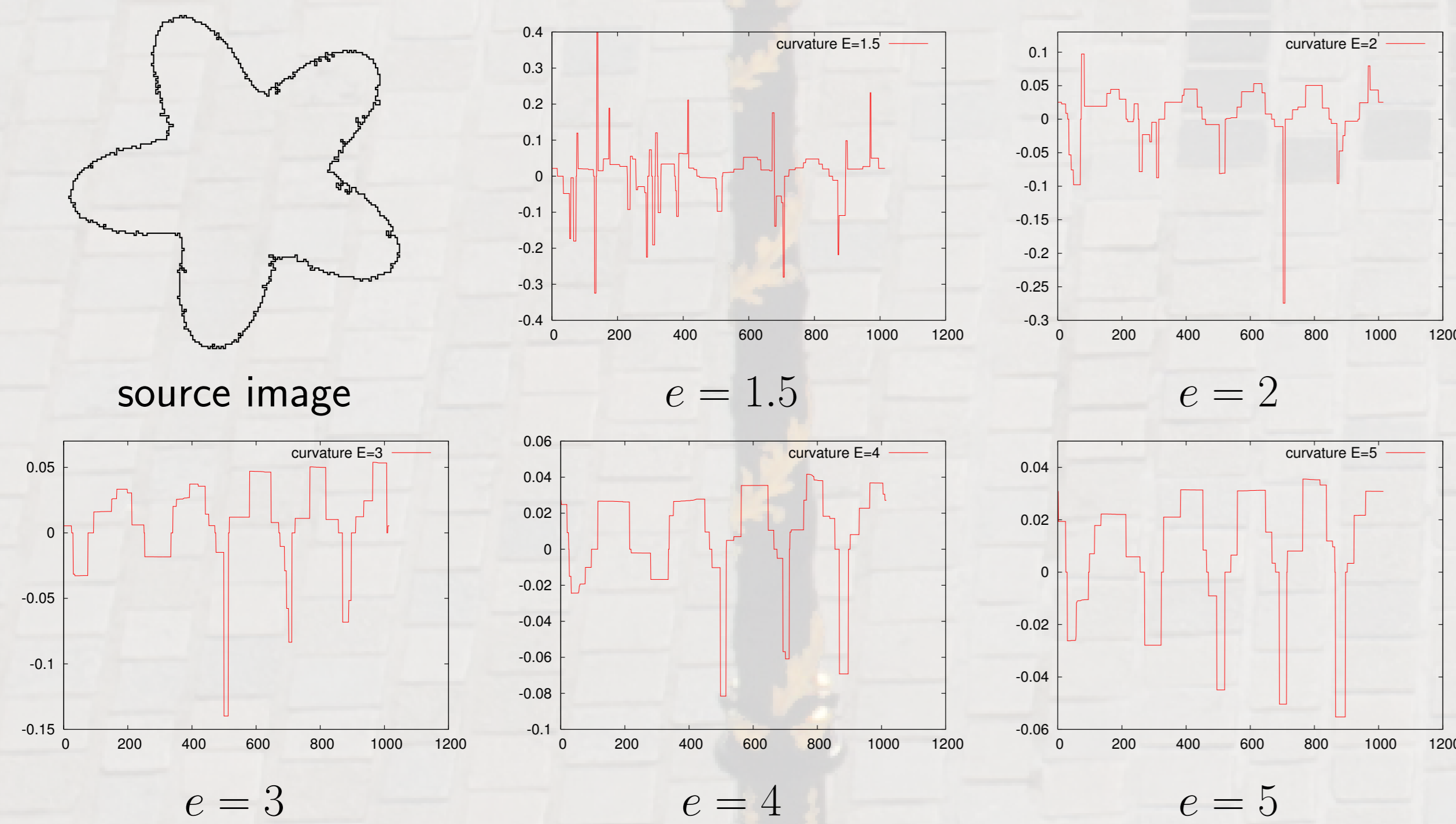
We propose an original strategy to detect locally both the amount of noise and the meaningful scales of each point of a digital contour. Based on the asymptotic properties of maximal segments, it also detects curved and flat parts of the contour. From a given maximal observation scale, the proposed approach does not require any parameter tuning and is easy to implement [2].

**Keyword:** Noise and meaningful scale detection, maximal segments.

## 1 Introduction

Motivation:

- Output quality/accuracy depends on the choice of the parameter.
- Relevance of a global parameter.
- Example: Geometric estimators (curvature, tangent), etc..

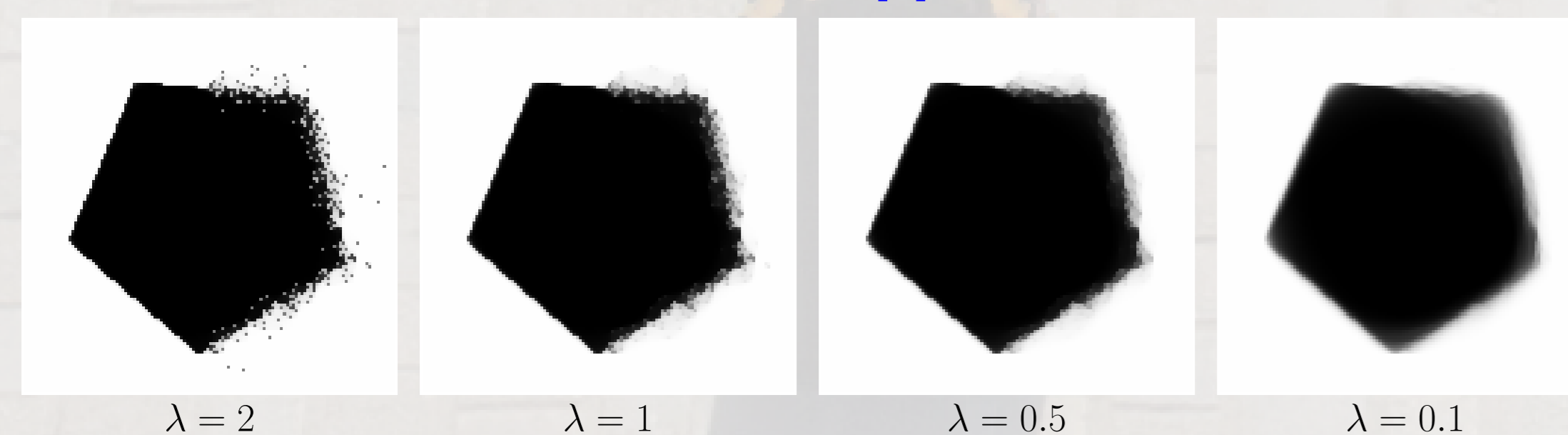


Few works are adapted for estimating and remove noise on binary images

- Morphological opening:



- Noise removal using Rudin *et al.* algorithm [4]:



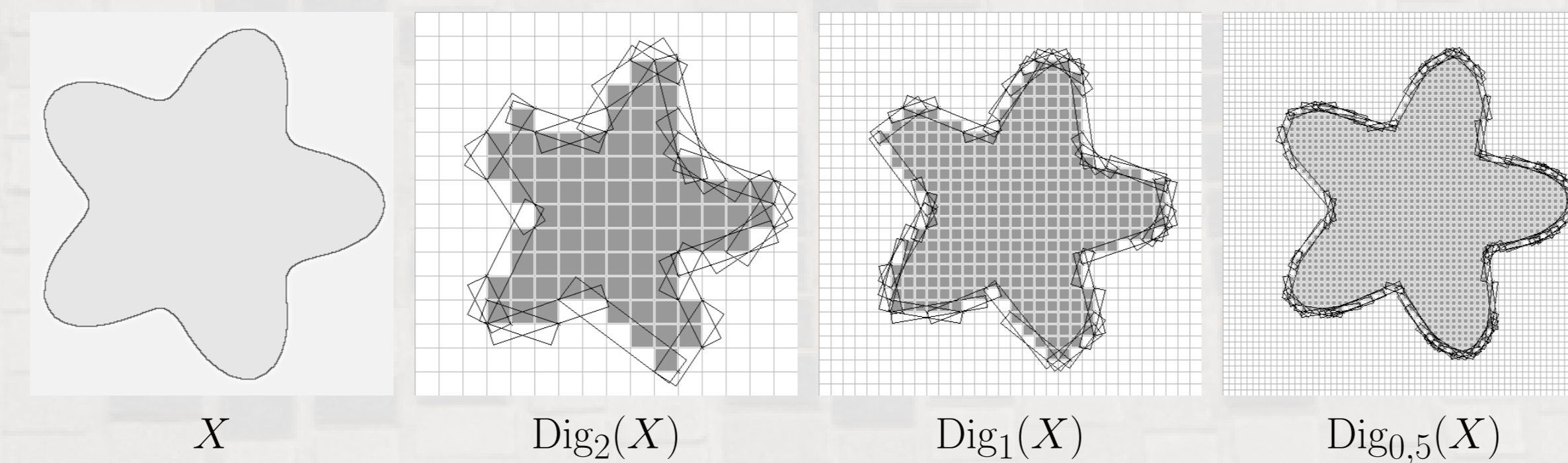
## 2 Scale properties of maximal segments

Main idea: Local shape analysis of digital contours

1. Exploit asymptotic properties of **perfect shape** digitizations.
2. Estimate them from a multiresolution decomposition of the **input shape**.
3. Compare them to determine a local meaningful scale.

### 2.1 Asymptotic properties of shape digitizations

- $X$  some simply connected compact shape of  $\mathbb{R}^2$
- $\text{Dig}_h(X)$  = Gauss digitization of  $X$  with step  $h$
- black boxes are the **maximal segments** of its boundary.
- they grow longer (in number of steps) as  $h$  gets finer.

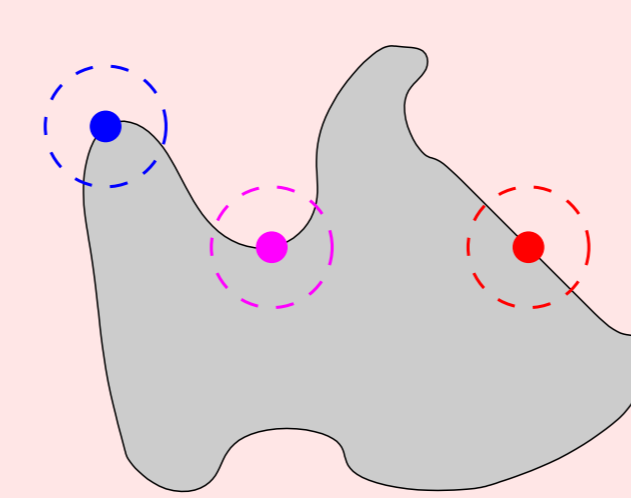


**Theorem [3]: asymptotic behavior of the length of maximal segments**

- $X$  simply connected shape in  $\mathbb{R}^2$  with piecewise  $C^3$  boundary  $\partial X$ ,
- $U$  an open connected neighborhood of  $p \in \partial X$ ,
- $(L_j^h)$  the digital lengths of the maximal segments of  $\text{Dig}_h(X)$  which cover  $p$ ,

$$\partial X \cap U \text{ strictly convex or concave, then } \Omega(1/h^{1/3}) \leq L_j^h \leq O(1/h^{1/2})$$

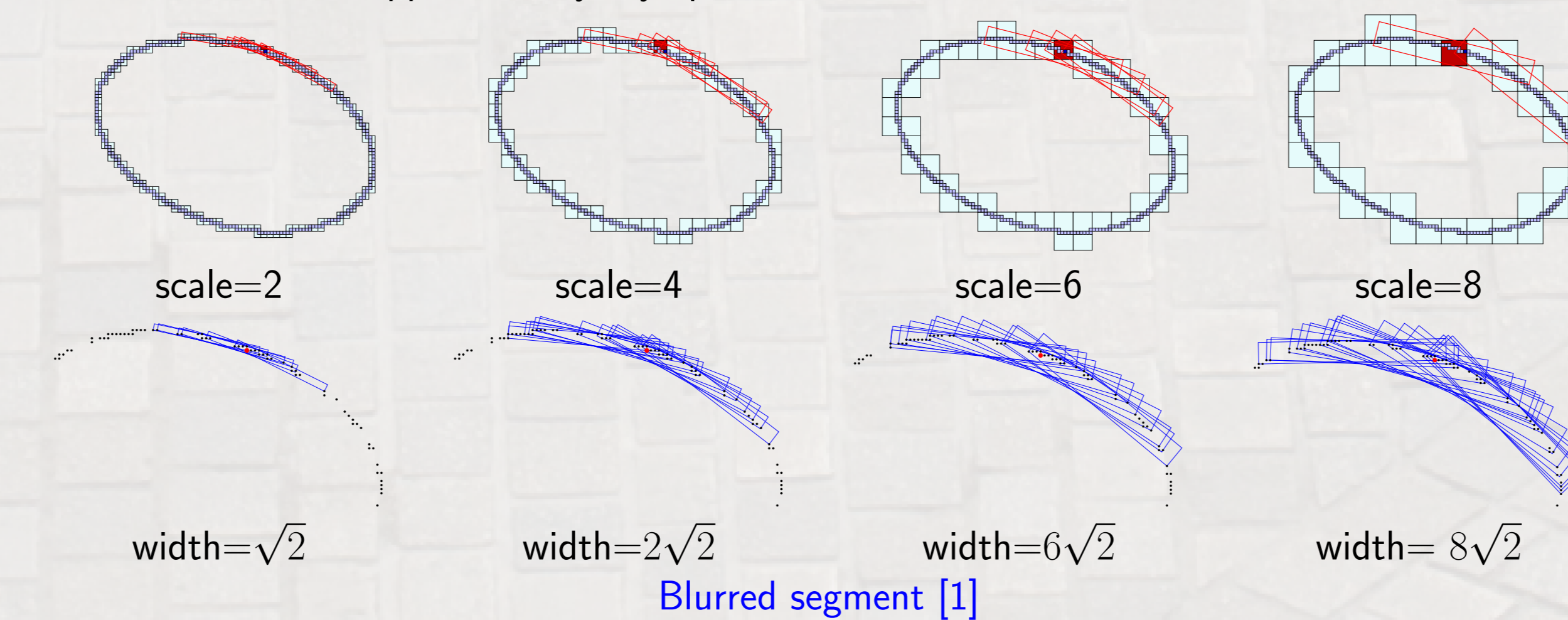
$$\partial X \cap U \text{ has null curvature, then } \Omega(1/h) \leq L_j^h \leq O(1/h)$$



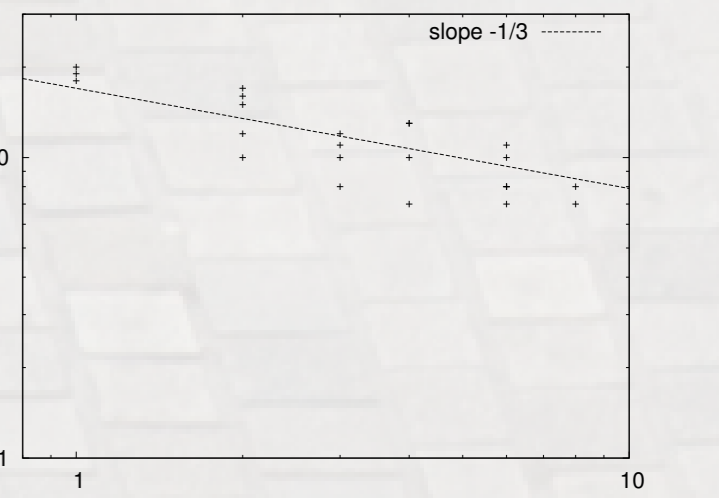
### 2.2 Asymptotic estimation with multiresolution

Main idea: : reverse asymptote with multiresolution

- Coarser and coarser sampling of the contour.
- Measure digital lengths of maximal segments.
- Should also follow approximately asymptotic behavior.



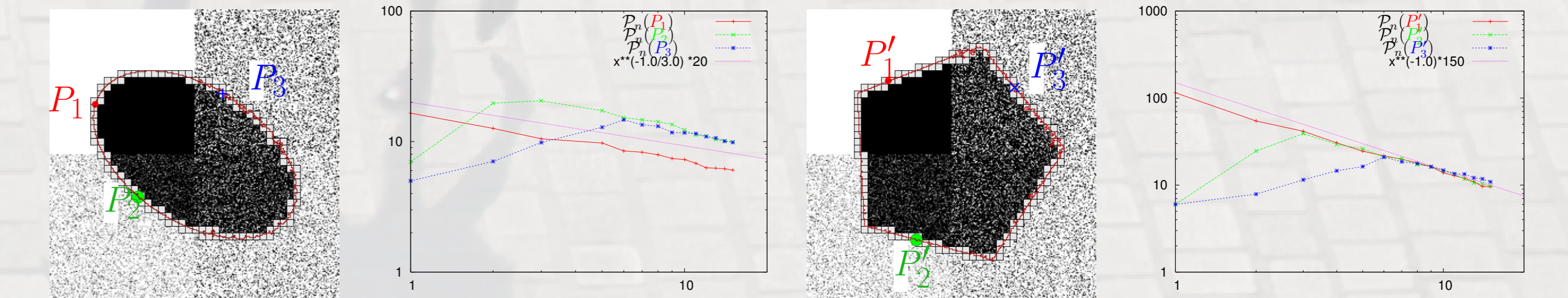
local shape geometry	$\text{length}(\frac{1}{h})$	slope log-scale
convex, concave	$\Omega((\frac{1}{h})^{1/3}) \leq \cdot \leq O((\frac{1}{h})^{1/2})$	$-\frac{1}{2} \leq \cdot \leq -\frac{1}{3}$
flat	$\Theta(\frac{1}{h})$	$\approx -1$
noise otherwise		



### 2.3 Meaningful scale

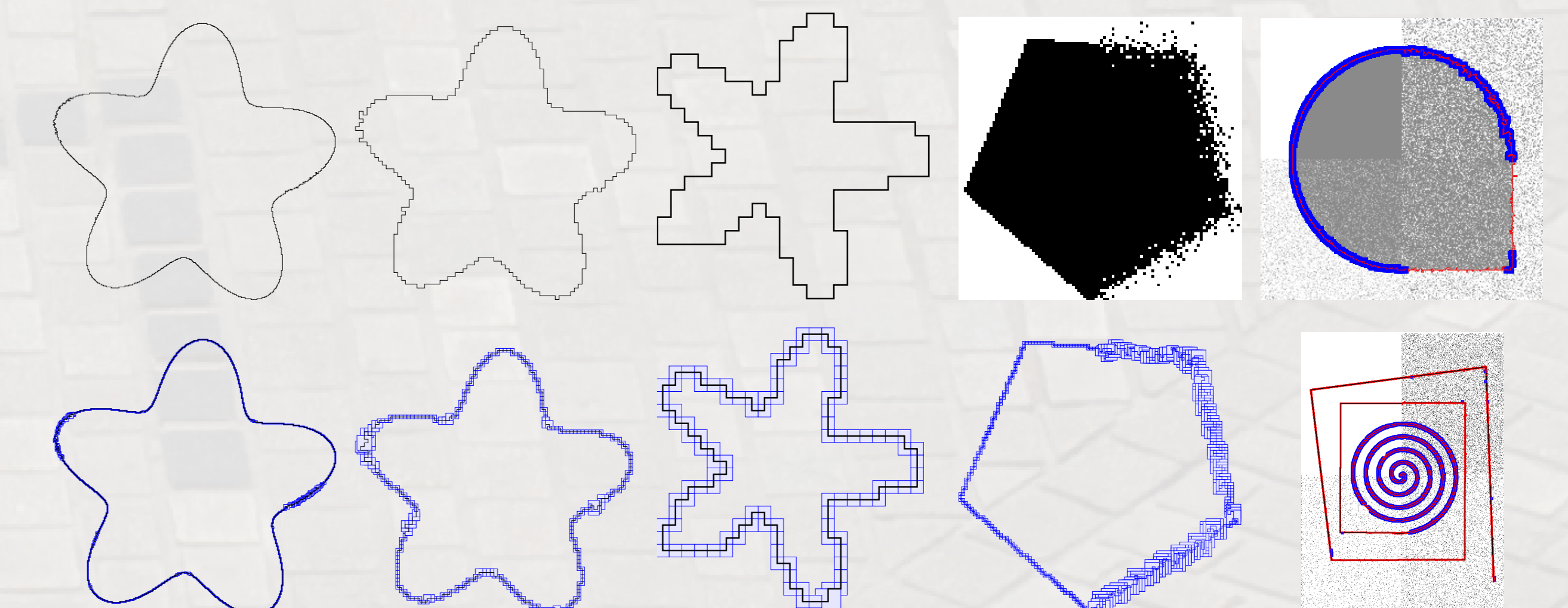
A **meaningful scale** of a multi-scale profile  $(X_i, Y_i)_{1 \leq i \leq n}$  is the pair  $(i_1, i_2)$   $1 \leq i_1 \leq i_2 \leq n$  such that for all  $i, i_1 \leq i < i_2$ :  $\frac{Y_{i+1} - Y_i}{X_{i+1} - X_i} \leq t_m$

while not true for  $i_1 - 1$  and  $i_2$  and  $t_m =$  noise threshold to discriminate curved from noisy areas.  
 $\Rightarrow$  If  $(i_1, i_2)$  is the first meaningful scale at point  $P$ , the **noise level** at point  $P$  is  $i_1 - 1$ .



## 3 Experiments

- Application on discrete contours



- Application with Blurred Segments on polygonal contour and extraction of meaningful contours:



## References

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